| Course Title | Linear Algebra | Course No. | MA511 |
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| Department | Mathematics | Structure (LTPC) | $3-1-0[4]$ |
| Offered for | M.Sc. Students | Type | Compulsory |
| Pre-requisite | None | To take effect from |  |

## Objectives

To give sufficient knowledge of the subject, which can be used by student for further applications in their respective domains of interest.

## Learning Outcomes

1. Concept of linear spaces, mapping between spaces, norm and their action on spaces.
2. Triangularization, diagonalization and Primary decomposition theorem.
3. Semi-simple operators, unitary and normal operators, spectral theory of normal operators.
4. Bilinear forms and Tensor products

## Contents

1. Vector Spaces over fields, subspaces, bases and dimension. Direct sum of the sub spaces, System of linear equations, Matrices and rank
2. Linear Transformations, Rank and Nullity theorem, Representation of linear transformations by matrices, duality and transpose.
3. Inner product spaces, Gram-Schmidt orthonormalization, orthogonal projections, linear functionals and adjoints, Hermitian, self-adjoint, Unitoary and normal operators, Spectral theorem for normal operators, Rayleigh quotient, Min-Max principle
4. Eigenvalues, Eigenvectors, Characteristic polynomials, minmal polynomials, Cayley Hamilton Theorem, triangulation, diagonalization, Jordan canonical forms, Bilinear forms, symmetric and skew-symmetric bilinear forms, positive definiteness
5. Applications of linear algebra

## Reference Books

1. Herstein, I. N. (1975) Topics in Algebra, $2^{\text {nd }}$ Edition, John Wiley \& Sons
2. Hoffman, K., and Kunze R. (1991) Linear Algebra, Prentice Hall of India
3. Lang, S. (2004) Linear Algebra, $3^{\text {rd }}$ Edition, Springer Verlag
4. Lax, P. (1997) Linear Algebra and its applications, John Wiley \& Sons, Indian Edition
5. Sharma, R. K., Shah, S. K. and Shankar, A. G. (2011) Algebra I: A Basic Course in Algebra, Pearson Education
